Simple solvation potential for coarse-grained models of proteins

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We formulate a simple solvation potential based on a coarsed-grain representation of amino acids

with two spheres modeling the C_{α} atom and an effective side-chain centroid. The potential relies on

a new method for estimating the buried area of residues, based on counting the effective number of

burying neighbours in a suitable way. This latter quantity shows a good correlation with the buried

area of residues computed from all atom crystallographic structures. We check the discriminatory

power of the solvation potential alone to identify the native fold of a protein from a set of decoys

and show the potential to be considerably selective.

Keywords: Protein folding, structure prediction, solvation, buried area

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INTRODUCTION

The prediction of three dimensional structure of the native state of proteins from the knowledge of their sequence of amino-acids can only be achieved if the interaction potentials among various parts of the peptide chain in the presence of solvent molecules are known to some extent. In fact, approaches to protein structure prediction are based on the thermodynamic hypothesis that the native state of a protein is the state of lowest free energy under physiological conditions [1]. Thus, the computation of the energy of a sequence in a given conformation would be the fundamental step toward the solution of the protein folding problem [2]. A rigorous approach [3] from "first principles" taking into account the quantum mechanics of a huge number of atoms constituting the protein is not practical and beyond actual computational capabilities. An usual way [4] to avoid dealing with too many microscopic degrees of freedom is to introduce a reduced representation of proteins in which each amino acid is represented by one or a few interaction sites. The main difficulty with such simplified representations is the need of an effective energy that captures, at least, the essential qualitative physical and chemical features of the folding process. This involves choosing the right contributions to the energy function as well as determining the related potentials [see for example 2.26-30].

Since the classical work of Kauzmann [5] it is evident [6] that the hydrophobic effect is one of the leading forces in the folding process. Hydrophobicity arises because the side-chain of some amino acids is not able to form hydrogen bonds with the surrounding water, and as a consequence its solubility is low. Gordon et al. [7] have reported a free energy difference associated with exposing such groups to water which is comparable with the strength of hydrogen bonds. Moreover, several experiments [8,9,10,11] have shown that non specific interaction and placement of hydrophobic residues is a critical determinant of protein structure.

Starting from the seminal work of Eisenberg and McLachlan [12] several efforts have been produced to model the hydrophobic effects [13-17] but a precise and computationally efficient method is still lacking. The purpose of this work is to cover this gap by developing a solvation energy for a coarse-grained model of a protein which is more accurate than the other existing ones but still is easy for numerical implementation in folding simulations. The energy function we propose is the sum over all the amino-acids of a contribution given by a factor proportional to the effective number of particles which are screening the amino-acid from its aqueous surroundings multiplied by an amino acid specific parameter measuring its hydrophobicity degree. These parameters are calculated through a statistical analysis on a training set of proteins.

An important test to validate any energy function is to check its ability to recognize native structures among a large number of well constructed decoys [18-21]. A number of standard decoy sets, consisting of the native structure plus a large ensemble of simulated protein-like structures have been established for benchmarking purposes [22]. The performance of our method on different test sets is better than other solvation energies [16,17] and is comparable to scoring functions which implicitly include other energetic contributions such as hydrogen bond, torsion angle and van der Waals potentials [23,24].

METHODS

In our model each residue is simplified as follows. The C^{α} atoms are represented by a sphere of radius 1.9 Å. The specific characteristic of each amino acid is captured by its side-chain which we again model as a sphere. The center of this sphere is located at the geometric center, $\mathbf{X_c}$, of all side chain atoms including the C_{β} atom, namely at:

$$\mathbf{X}_c = \frac{\sum_{l=1}^m \mathbf{X}_l}{m}.$$

where $\mathbf{X_l}$ are the positions of all the atoms in the given side chain and m is the total number of atoms in the side chain. The radius r_c of the side-chain sphere is defined as the root mean square deviation of the position of the side-chain atoms of that residue from $\mathbf{X_c}$. Relative changes in positions of side chain atoms of a particular residue in various proteins are reflected in the corresponding change in position of the side-chain center and in some fluctuation of the side change radius. Since modeling side chains as spheres is a gross simplification of side chain geometry, the slight overlap of different sphere pairs can occur. Note that throughout this paper we do not enforce any steric constraint.

Our main purpose is to find a way within this representation to compute the effective number N_i^a of spheres (both C^{α} and side chains) which are burying the side chain of the amino-acid of type a, located at position i along the chain, from the solvent. This number will then be used as an estimation of the buried area of residue i in order to define a solvation energy in this coarse-grained perspective. Let us call D_{jk} the distance between two generic spheres j and k (note the difference between indexes j, k going through both C^{α} and side chains and residue index i going only through side chain spheres). All other spheres in the chain, either C^{α} or side chains, contribute to N_i^a through the relation:

$$N_i^a = \sum_{\substack{j \notin i \\ j \notin i \pm 1}} B_{ij} S_{ij} \tag{1}$$

where the sum is running only through spheres belonging to residues not adjacent to i. B_{ij} represents the bare contribution by sphere j to the protection of side chain i from water and it is equal to 1 if the distance D_{ij} is smaller than $R_{ij} = r_i + r_j + \frac{r_{\text{water}}}{2}$ ($r_{\text{water}} = 1.4$ Å is the radius of a water molecule) or $\frac{R_{ij}}{D_{ij}}$ otherwise. The threshold R_{ij} has been chosen to discriminate between two regimes. If $D_{ij} < R_{ij}$, a portion of the surface area of side chain i is screened from contact with water molecules, since the latter can only marginally accommodate between side chain i and sphere j (see Fig. 2). If $D_{ij} > R_{ij}$, this constraint disappears but in order to take into account fluctuations, due to the varying geometry of side chains and to the simple assumption of spherical geometry, we assume the screening effect to be still present and decaying as $\frac{1}{d}$.

 S_{ij} instead takes into account the fact that the screening effect of sphere j on side chain i can be already accounted for by the presence of other spheres of the chain. We define S_{ij} as

$$S_{ij} = \prod_{\substack{k \neq j \\ k \notin i, i \pm 1}} S_{ij}^k$$

where we multiply the individual contributions S_{ij}^k of different spheres to the overlap of screening effects, given by

$$S_{ij}^{k} = \left\{ \begin{array}{ll} (1 - M_{ijk}) \frac{r_{j}}{r_{k}} & \text{if } M_{ijk} > 0.7 \\ 1 & \text{if } M_{ijk} \le 0.7 \text{ or } D_{ij} \le D_{ik} \end{array} \right\}$$

The coefficients M_{ijk} are defined as

$$M_{ijk} = \frac{D_{ij}}{D_{ik} + D_{ki}}$$

The $M_{ijk}=1$ limit corresponds to a complete overlap of the screening effects (Fig.2c) so that in this case $S_{ij}^k=0$; sphere j is not contributing effectively in screening side chain i from water molecules more than sphere k is already doing. It is easy to demonstrate that when three spheres of equal size are in contact with each other, M_{ijk} is equal to 0.5 (e.g. see Fig.2a). In such a situation no sphere is actually obstructing the other two to come in complete contact and there is no overlap of the screening effects. Starting from such a limiting geometry, when sphere k^{th} is inserting between the other two (Fig.2b) the value of M_{ijk} is increasing. The choice of 0.7 as the lower limit to measure the screening overlap has been made based upon an optimization procedure. The factor $\frac{r_j}{r_k}$ takes into account the fact that the bigger r_k the more overlapping the screening effects of j and k, and therefore the smaller S_{ij}^k . It is interesting to note that statistics of side chain sizes, based on our coarse-grained representation, reveals that the ratio r_j/r_k is generally less than 3. So, $1 \geq M_{ijk} > 0.7$ never let contributions to S_{ij}^k be bigger than unity.

To test our method we use the Top500H database [31] of non-redundant protein structures. It is a hand-curated set of 500 high-resolution structures all solved by X-ray crystallography to 1.8 Å or better resolution. From this database, only those 220 proteins which do not have any discontinuity in the chain have actually been selected. The analysis of this proteins shows that the effective number of contacts is ranging from 0 to about 12 (see Fig. 3). We took 10 to be the upper limit in all further calculation since it was already shown to be roughly the number of neighbours with which an amino-acid becomes buried (see, e.g. [17,32]). Our way of taking into account the overlap of different screening effects could indeed produce some overcounting and whenever the counting of N_i^a is above 10, it is put equal to it. To check the correspondence between N_i^a and buried area, we have calculated the buried area of residues of these proteins by using on-line available program 'GETAREA 1.1' [34] (URL: http://www.scsb.utmb.edu/cgi-bin/get_a_form.tcl). The number B_i^a that we use from this program is the percentage of buried side-chain surface area with respect to the "random coil" value per residue. The "random coil" value for residue is the average solvent-accessible surface area of a in the tripeptide Gly - a - Gly in an ensemble of 30 random conformations. B_i^a varies from 0% (completely exposed) to 100% (fully buried) and it is plotted in Fig.3 against N_i^a for all amino-acids of a set of proteins (see Results for discussions). The average buried area \overline{B}^a of each residue kind is displayed in Table A.

In order to develop the solvation energy we consider the amino-acids to be hydrophobic if their average buried area is more than 60%, otherwise we take them to be polar. The solvation energy parameters E_a for different residue types, listed in Table A, are obtained through the relation:

$$E_a = (60 - \bar{B}^a)/(\bar{B}_{max} - 60)$$

where $\bar{B}_{max} = max\{\bar{B}^a\} = 86.90\%$. In our coarse-grained representation the overall solvation energy is then obtained summing contribution from all residues, negative for hydrophobic ones $(E_a < 0)$, and positive otherwise, which are proportional to the residue buried area N_i^a evaluated from Eq. (1):

$$E_{solv} = \sum_{i} E_a \times N_i^a, \tag{2}$$

Note that no solvation energy is associated to GLY in our model, but it takes part into the calculation of solvation energy of other residues by virtue of its C^{α} sphere.

Five different performance measures have been applied to assess the ability of our solvation potential in discriminating the native structure from native like ones. The Rank1 measure is the one which is more direct in the sense it tells us about the position of the native state among the decoys in an arrangement of increasing order of their energy. So, Rank1 being equal to 1 means the native fold is the lowest energy conformation among the decoys. We also employ the Z-score which is defined as

$$Z - \text{score} = \frac{E_{native} - \bar{E}}{\sigma}$$

where, E_{native} is the energy of the native fold and \bar{E} is the average energy of decoys with a standard deviation σ . We also employ additional performance measures to understand the discriminatory capacity of our potential for native like structures rather than oly for the native fold. To assess such properties we use logPB1, logPB10 and F.E. (fraction enrichment) [33] measures to see how the present potential fares. logPB1 is the log probability of selecting the best scoring conformation and is given by

$$logPB1 = log_{10}\left(\frac{R_i}{p}\right)$$

where R_i is the RMSD rank of the best scoring conformation in p decoys. logPB10 is the probability of selecting the lowest RMSD conformation among the 10 best scoring conformations ($R_i = min\{R_1, ..., R_{10}\}$). The F.E. or fraction enrichment is the percentage of the top 10% lowest RMSD conformations in the top 10% best scoring conformations.

RESULTS

Our first test aims to verify the existence of a correlation between the method, presented in the previous section, of counting effective neighbours (N_i^a) of an aminoacid and its buried area. To perform this test, we have used the Top500H database [31] of non-redundant protein structures selecting only those proteins which do not have any discontinuity in the chain. Fig.3 shows a plot of the calculated buried area, obtained using $GETAREA\ 1.1$, of different residues in their native conformations versus their N_i^a . The correlation turns out to be quite good (coefficient of correlation = 0.89).

The crucial test for our method consists, however, in assessing the ability of the solvation energy based on Eq. (2) to discriminate between native states and not native decoy conformations for the same sequence. A good decoy set must include a large number of conformations, some near native and other that are native-like in all respects except the overall folded conformation and this set should be generated independently from the evaluated scoring mechanisms to avoid bias toward any particular selection methodology. Our solvation potential has been tested on four such standard decoy sets: 4state_reduced, lattice_ssfit, lmds sets from the Decoys 'R' Us web sites (http//:dd.stanford.edu and http//:ddcompbio.washington.edu) and the Rosetta decoys from the Baker laboratory site (http//:depts.washington.edu/bakerpg).

In Table B we arrange the average scores for the different sets whereas the detailed account of the individual scores for every target in various decoy sets are given in Tables C-F. This detailed scores are more revealing than the average ones due to the fact that some targets which are scoring particularly bad due to some specific reasons can affect the average score.

For the $4state_reduced$, we observe that Rank1 = 1 four times out of seven (4/7). It is 2 for the protein 2cro

whereas 5 and 4 for the proteins 4pti and 4rxn, respectively. Protein 4pti has three disulphide bonds which might be in conflict with the optimum arrangement on the basis of solvation energy alone. This performance can be compared with other two solvation potentials: the one called *Chebyshev-expanded hydrophobic* potential (CHP) introduced by Fein, Xia and Levitt [17] and the one introduced by Jones [16] (SOLV) used by Tosatto [25] to formulate a combined potential function called FRST. The discriminatory predictions of CHP, SOLV and FRST as well (although is not a solvation potential) are reported in table G and H for the available sets and with the available information. For the $4state_reduced$ set, both CHP and SOLV get Rank = 1 only in one case and both methods with a worse average value for the parameter Z-score.

For the $lattice_ssfit$ set of decoys we obtain Rank1 = 1 in 6 cases out of 8. Again the performance is much better of SOLV (there are not available data for CHP) which has Rank1 = 1 in 4 cases out of 8, and worse values for the Z-score, logPB1, logPB10 and F.E. parameters. In this set, the targets for which our method gives $Rank1 \neq 1$ are the proteins 1dkt - A and 1trl - A: these two proteins are a part of a whole chain. The missing parts might have residues which contribute to the count of N_i^a . Their absence can drastically reduce the efficiency of the methods.

For the set of decoy lmds, Rank1 = 1 in 4 proteins out of 8. The proteins 1b0n-B and 1fc2 are the ones which show almost no selection on the basis of this solvation potential because they are short chains of hetero-dimers. Other two, 2ovo and 4pti, have three disulfide bonds. Interestingly, 4pti has a Rank1 measure of the same order also in the decoy sets $4state_reduced$ and Rosetta. Again the performance is much better than for the other two solvation energy potentials.

For the set Rosetta, Rank1 = 1 in 17 cases out of 23. In this collection of decoys, there are proteins which have residues clipped from the chain end and thus decoys are considerably shorter than the actual protein. We have selected those targets from Rosetta which have at most up to 8 residues clipped from the end of a chain (in Table F the numbers within bracket just after the target name are the numbers of residues clipped). We are not considering those having more residues clipped since it can affect proper calculation of solvation energy. It is important to note that the targets for which the Rank1 measure is not very good are mainly those which have a large number of residues clipped, even though some of the latter have Rank1 = 1. We can not compare our method on this decoys set with CHP and SOLV since these data are not available. Nevertheless, we make a comparison with an all atom-atom contact scoring energy proposed by McConey et al. [23] which has a record for Rank = 1 of 19 out of 23 with a Z – score = -3.6, performances which are just slightly better of ours. Keeping in mind that the approach in [23] is

taking care in detail of various interactions with more than 28000 parameter it turns out that our solvation energy has a very high degree of confidence in discriminating native state with respect to other methods.

For all the set in which is possible to make a comparison the full algorithm FRST is performing better than our method, although sometimes the values of the less selective parameters logPB1, logPB10, and F.E are comparable. This is a consequence of the fact that FRST is an algorithm which combine four different knowledge based potentials. In addition to the solvation potential (SOLV), there are the pairwise, the hydrogen bond and the torsion angle potentials. The results we present here suggest that, regarding the development of refined methods for structure recognition, it should be convenient to include our method rather than SOLV in the FRST algorithm.

DISCUSSION

In the present work we have proposed a simple and efficient method to estimate the buried area of a side chain group by counting the effective number of atoms which are screening it from water. This evaluation builds on the assumption of spherical symmetry of the interacting side chain groups. It corrects for this oversimplification by allowing the screening effect to be considered beyond the range dictated by sphere sizes and by considering the three-body contribution to its cooperativity. The resulting quantity is well related to the buried area and it can be used to compute a solvation energy which is based just on 20 energy solvation parameters, one for each kind of amino-acid. This solvation energy works pretty well, better than any other solvation energy, in recognizing native structures among set of well constructed, alternative decoys. The use of a small number of parameters makes our solvation potential more physically transparent than other elaborate knowledge based energy functions with a much larger parameter space.

The targets which are parts of larger chain, or have a good number of residues clipped from the chain end or having many disulfide bonds etc are generally those for which the present solvation potential fails to identify the native fold.

Our potential does not implicitly include any other interaction than the solvation effect, so it should be easily improved by combining it with other interaction terms. Moreover, since the model we use to represent amino-acids is quite simplified, the approach can be easily implemented in ab-inito simulation of protein folding.

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Table A: Data showing average measure of buried area for Amino acids in native state's database

Amino acid	\overline{B}^a	E_a
ALA	71.55	-0.39
ARG	59.57	0.01
ASN	58.77	0.04
ASP	55.87	0.14
CYS	89.80	-1.00
GLN	57.46	0.09
GLU	50.44	0.32
HIS	70.12	-0.34
ILE	86.90	-0.90
LEU	85.48	-0.86
LYS	44.30	0.53
MET	81.92	-0.74
PHE	86.82	-0.90
PRO	57.34	0.09
SER	61.94	-0.07
THR	65.91	-0.20
TRP	84.95	-0.84
TYR	80.36	-0.68
VAL	85.36	-0.85

Table B: Average performance measures

Decoy Set	Rank 1	Z-score	logPB1	logPB10	F.E.
4state_reduced	4/7	-2.89	-1.19	-1.88	0.28
lmds	4/8	-2.75	-0.48	-1.36	0.14
lattice_ssfit	6/8	-4.06	-0.41	-1.55	0.12
rosetta	17/23	-3.44	-0.54	-1.65	0.16
Total/average	31/46	-3.28	-0.85	-1.61	0.17

Table C: Performance Measure for 4state_reduced

Target	Rank 1	Z-score	logPB1	logPB10	F.E.
1ctf	1	-3.53	-2.10	-2.10	0.55
1r69	1	-3.68	-1.93	-2.53	0.27
$1 \mathrm{sn} 3$	1	-2.52	-0.27	-1.09	0.10
2cro	2	-3.01	-1.26	-2.53	0.32
3icb	1	-2.26	-2.12	-2.12	0.46
4pti	5	-2.51	-0.50	-1.48	0.06
4rxn	4	-2.71	-0.15	-1.88	0.20
Total/average	4/7	-2.89	-1.19	-1.88	0.28

Table D: Performance Measure for lmds (* excluded from the calculation of averages. We have not considered the score of the targets 1b0nB and 1fc2 while calculating the averages.)

Target	Rank 1	Z-score	logPB1	logPB10	F.E.
1b0n-B*	439	1.18	-0.01	-0.32	0.04
1ctf	1	-3.42	-0.36	-0.77	0.08
1fc2*	409	0.91	-0.31	-2.22	0.07
1igd	1	-2.87	-0.25	-1.39	0.14
1shf-A	1	-2.90	-0.14	-1.09	0.09
2cro	1	-3.42	-0.60	-1.37	0.18
2ovo	16	-1.67	-1.00	-1.46	0.14
4pti	6	-2.24	-0.53	-2.06	0.20
Total/average	4/8	-2.75	-0.48	-1.36	0.14

Table E: Performance Measure for lattice_ssfit

Target	Rank 1	Z-score	logPB1	logPB10	F.E.
1ctf	1	-5.04	-0.06	-0.68	0.14
1beo	1	-3.67	-0.36	-1.13	0.12
1dkt-A	8	-2.73	-0.20	-2.35	0.11
1fca	1	-7.38	-2.45	-2.45	0.09
1nkl	1	-4.54	-0.01	-2.52	0.08
1pgb	1	-4.01	-0.10	-0.51	0.10
1trl-A	101	-1.61	-0.12	-0.98	0.18
4icb	1	-3.50	-0.01	-1.75	0.12
Total/average	6/8	-4.06	-0.41	-1.55	0.12

Table F: Performance Measure for rosetta (* excluded from the calculation of averages)

Target	Rank 1	Z-score	logPB1	logPB10	F.E.
1aa2(3)	1	-4.18	-0.65	-1.70	0.15
1acf(2)	1	-5.34	-0.31	-2.15	0.23
1bdo(5)	1	-3.81	-0.03	-1.55	0.14
1cc5(7)*	407	-0.30	-0.12	-1.06	0.12
1csp(3)	1	-2.73	-0.18	-2.52	0.20
1ctf (1)	1	-3.49	-0.06	-1.34	0.14
1eca(4)	1	-3.67	-0.21	-2.00	0.13
1erv (0)	1	-4.20	-0.56	-3.00	0.21
1kte(5)	1	-2.67	-1.55	-1.55	0.12
1lfb(8)	40	-1.47	-0.97	-1.68	0.12
1 mbd(6)	1	-4.37	-1.25	-1.44	0.14
1 msi(5)	1	-4.61	-1.10	-2.00	0.15
1pal(8)	4	-2.07	-0.25	-1.92	0.14
1pdo(8)	1	-3.79	-0.90	-1.33	0.20
1ptq(7)*	595	0.19	-0.81	-1.35	0.15
1r69(2)	1	-2.90	-1.23	-1.72	0.16
1ris(5)	12	-1.75	-0.57	-1.65	0.18
1tul(5)	1	-3.40	-0.31	-1.52	0.16
1vls (3)	1	-2.78	-0.62	-1.82	0.19
1who (6)	1	-3.56	-0.21	-0.79	0.19
2acy(6)	1	-4.75	-0.25	-1.74	0.15
2gdm(5)	1	-3.55	-0.07	-1.24	0.13
5pti(3)	2	-3.25	-0.25	-0.81	0.07
Total/average	17/23	-3.44	-0.54	-1.65	0.16

Table G: Comparison with Chebyshev-Expanded hydrophobic potential (CHP) for the decoy sets 4state_reduced and lmds. The data separated by colons are our score: CHP score

4state_reduced				lmds	
target	Rank 1	Z-score	target	Rank 1	Z-score
1ctf	1:1	-3.53:-2.9	1ctf	1:1	-3.42:-3.5
1r69	1:2	-3.68:-2.4	1 fc 2	409:9	0.91:-2.1
$1 \mathrm{sn} 3$	1:3	-2.52:-2.1	1igd	1:1	-2.87:-2.8
2cro	2:60	-3.01:-1.3	1shf-A	1:n/a	-2.90:n/a
3icb	1:10	-2.26:-1.6	2cro	1:250	-3.42:-0.4
4pti	5:62	-2.51:-1.7	2ovo	16:7	-1.67:-2.2
4rxn	4:6	-2.71:-2.2	4pti	6:32	-2.24:-1.4

Table H: Comparison with SOLV and FRST. The data separated by colons are $our\ score: SOLV$ $score: FRST\ score$

decoy set	Rank 1	Z-score	logPB1	logPB10	F.E.
4state_reduced	4/7:1/7:7/7	-2.89:-1.7:-4.4	-1.19:-0.51:-1.62	-1.88:-1.78:-2.31	0.28:0.28:0.43
lattice_ssfit	6/8:4/8:8/8	-4.06:-3.2:-6.7	-0.41:-0.37:-0.58	-1.55:-1.20:-1.29	0.12:0.10:0.10
lmds	4/8:2/8:6/8	-2.75:-1.2:-3.5	-0.48:-0.49:-0.48	-1.36:-1.46:-1.44	0.14:0.15:0.14

Figure Caption

Figure 1. A schematic diagram to show the quantities involved in the calculation of of M_{ijk}

Figure 2. A schematic diagram to show the calculation of M_{ijk} for equal sized spheres. Fig.2a corresponds to the limiting case $M_{ijk}=0.5$ whereas Fig.2c presents $M_{ijk}=1$ upper limit. The Fig.2b is intermediate between the above mentioned limits, namely $M_{ijk}=0.64$

Figure 3. A plot to compare effective number of neighbours to a residue with its actual buried area obtained by using GETAREA





